

General Certificate of Education Advanced Subsidiary Examination January 2010

Mathematics

MPC2

Unit Pure Core 2

Monday 11 January 2010 9.00 am to 10.30 am

For this paper you must have:

- an 8-page answer book
- the blue AQA booklet of formulae and statistical tables.
 You may use a graphics calculator.

Time allowed

• 1 hour 30 minutes

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Write the information required on the front of your answer book. The **Examining Body** for this paper is AQA. The **Paper Reference** is MPC2.
- Answer all questions.
- Show all necessary working; otherwise marks for method may be lost.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

Advice

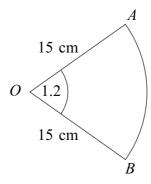
• Unless stated otherwise, you may quote formulae, without proof, from the booklet.

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Answer all questions.

1 The diagram shows a sector OAB of a circle with centre O.



The radius of the circle is 15 cm and angle AOB = 1.2 radians.

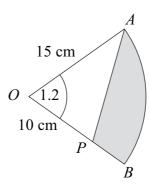
(a) (i) Show that the area of the sector is 135 cm².

(2 marks)

(ii) Calculate the length of the arc AB.

(2 marks)

(b) The point P lies on the radius OB such that OP = 10 cm, as shown in the diagram below.



Calculate the perimeter of the shaded region bounded by AP, PB and the arc AB, giving your answer to three significant figures. (5 marks)

2 At the point (x, y) on a curve, where x > 0, the gradient is given by

$$\frac{\mathrm{d}y}{\mathrm{d}x} = 7\sqrt{x^5} - 4$$

- (a) Write $\sqrt{x^5}$ in the form x^k , where k is a fraction. (1 mark)
- (b) Find $\int (7\sqrt{x^5} 4) dx$. (3 marks)
- (c) Hence find the equation of the curve, given that the curve passes through the point (1, 3). (3 marks)
- 3 (a) Find the value of x in each of the following:

(i)
$$\log_0 x = 0$$
; (1 mark)

(ii)
$$\log_9 x = \frac{1}{2}$$
. (1 mark)

(b) Given that

$$2\log_a n = \log_a 18 + \log_a (n-4)$$

find the possible values of n.

(5 marks)

4 An arithmetic series has first term a and common difference d.

The sum of the first 31 terms of the series is 310.

(a) Show that
$$a + 15d = 10$$
. (3 marks)

- (b) Given also that the 21st term is twice the 16th term, find the value of d. (3 marks)
- (c) The *n*th term of the series is u_n . Given that $\sum_{n=1}^k u_n = 0$, find the value of k. (4 marks)

- 5 A curve has equation $y = \frac{1}{x^3} + 48x$.
 - (a) Find $\frac{dy}{dx}$. (3 marks)
 - (b) Hence find the equation of each of the two tangents to the curve that are parallel to the *x*-axis. (4 marks)
 - (c) Find an equation of the normal to the curve at the point (1, 49). (3 marks)
- 6 (a) Sketch the curve with equation $y = 2^x$, indicating the coordinates of any point where the curve intersects the coordinate axes. (2 marks)
 - (b) (i) Use the trapezium rule with five ordinates (four strips) to find an approximate value for $\int_0^2 2^x dx$, giving your answer to three significant figures. (4 marks)
 - (ii) State how you could obtain a better approximation to the value of the integral using the trapezium rule. (1 mark)
 - (c) Describe a geometrical transformation that maps the graph of $y = 2^x$ onto the graph of $y = 2^{x+7} + 3$.
 - (d) The curve $y = 2^{x+k} + 3$ intersects the y-axis at the point A(0, 8). Show that $k = \log_m n$, where m and n are integers. (2 marks)
- 7 (a) The first four terms of the binomial expansion of $(1+2x)^7$ in ascending powers of x are $1+ax+bx^2+cx^3$. Find the values of the integers a, b and c. (4 marks)
 - (b) Hence find the coefficient of x^3 in the expansion of $\left(1 \frac{1}{2}x\right)^2 (1 + 2x)^7$. (4 marks)

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- 8 (a) Solve the equation $\tan(x + 52^\circ) = \tan 22^\circ$, giving the values of x in the interval $0^\circ \le x \le 360^\circ$. (3 marks)
 - (b) (i) Show that the equation

$$3\tan\theta = \frac{8}{\sin\theta}$$

can be written as

$$3\cos^2\theta + 8\cos\theta - 3 = 0 (3 marks)$$

(ii) Find the value of $\cos \theta$ that satisfies the equation

$$3\cos^2\theta + 8\cos\theta - 3 = 0 (2 marks)$$

(iii) Hence solve the equation

$$3\tan 2x = \frac{8}{\sin 2x}$$

giving all values of x to the nearest degree in the interval $0^{\circ} \leqslant x \leqslant 180^{\circ}$.

(4 marks)

END OF QUESTIONS

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